

□ *Interior of a subset of \mathbb{X}* : Given any $S \subseteq X$, the interior of S in \mathbb{X} is

- the largest open set $In_X(S)$ such that
- $In_X(S) \subseteq S$.

□ *Boundary of a subset of \mathbb{X}* : Given any $S \subseteq X$, the boundary of S in \mathbb{X} is

- $Cl_X(S) - In_X(S)$.

□ *Convergent sequence in \mathbb{X}* : A sequence $\{x^m\} \in X^\infty$ converges to $x^* \in \mathbb{X}$ if

- for each $\epsilon > 0$
- \exists a real number $M(\epsilon)$ such that
- $d(x^m, x^*) < \epsilon$
- $\forall m \geq M(\epsilon)$.

□ *Closed subset of \mathbb{X}* : A subset S is closed in \mathbb{X} if, and only if,

- any sequence all of whose terms are in S
- converges to a point in S , if it converges at all.

□ *Bounded subset of \mathbb{X}* : A subset S is bounded in \mathbb{X} if

- $\exists \epsilon > 0$ such that
- $S \subseteq N_{\epsilon, X}(x)$
- for some $x \in S$.

□ *Connected subset of \mathbb{X}* : A subset S is connected in \mathbb{X} iff

- S can not be written as $S \equiv S_1 \cup S_2$
- where $S_1 \cap S_2 = \emptyset$
- and S_1, S_2 are open in S .

□ *Connected Metric Space \mathbb{X}* : \mathbb{X} is connected iff the only clopen subsets of \mathbb{X} are \mathbb{X} and \emptyset .

□ *Dense subset of \mathbb{X}* : A subset Y is said to be dense in \mathbb{X} if

- $Cl_X(Y) = X$.